

# The Magneto-thermal Analysis of A High Torque Density Joint Motor for Humanoid Robots

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**Abstract**—The high power capacity of humanoid robot is desired for application of running or jumping motions, and the new generation robot formulate the need for a low-mass high-torque motor. A frameless motor has been designed by the group, it is very important to calculate the thermal field of the motor and get the conclusion for the choice of the motor parameters. The magneto-thermal coupling analysis of the motor was carried out based on the thermal network by the iterative calculation. By using the equivalent thermal network method, the elements copper loss and core loss is coupled into elements in thermal analysis by keeping the same mesh structure between magnetic and thermal analysis. Other losses such as air friction loss, rotor loss are included in the model. A temperature rise calculation program was written and different position temperature distribution was obtained. In the meantime, the steady-state temperature of BLDC was calculated by using the finite element method (FEM). The experimental results show that, the actual torque performance of the motor can reach the target of our design, at last, temperature calculation results obtained from two different methods were compared with experimental data, and the correctness of the calculation model is verified.

## I. INTRODUCTION

Improvement of performance of robots has necessitated technological advances in control algorithms, mechanical structures, and electric machines. The humanoid robot joint electromotive motor is used in permanent magnet brushless DC motor which is studied as a key point in recently [1][2]. This kind of permanent magnet motor eliminates the shortage of DC motors, at same time, with the characteristics of low consumption, compact structure, high efficiency and high reliability [3][4]. The Fig. 1 is the BHR-6 robot which is built by the group[5][6], the robot achieve walking, falling, crawling, and rolling. The group has the goal of building the faster humanoid robot, even running and jumping, so it presented challenges in the area of electric machinery in particular. One of the limitations in achieving the goal is the torque used to power the robot, as well as the mass and power dissipation. The Group want to improve torque and reduce the gear requirement, therefore, it is optimal to high torque density and low gear ratio requirement, these

limitations formulate the need for a low-mass high-torque motor.



Fig. 1. BHR-6 robot

A frameless permanent magnet brushless DC motor with fractional slot concentrated winding has been designed by the Group. While working at the rated current, the rated torque of the motor output is 1.25 Nm and the weight of the motor is 342g, therefore the torque density of the designed machine is 3.65Nm/kg, moreover, the peak torque of the motor is 4.2Nm. Fig. 2 shows the data which is collected from some commercial motors such as Maxon motors and Kollmorgen motors and Parker motors to evaluate the scaling predictions. From Fig. 2, the torque density of the commercial motors which used by the Group is no more than 2.6Nm/kg. Because the continuous torque represents the motor thermal characteristics, so it is used as a representative metric [7][8]. The torque data of the motor which is designed in this paper is compared with the torque data which has been shown in Fig. 2. From the result, the torque density is two to three times than that of the commercial motor currently used by the Group.

The flux density and the current density of the motor must be designed more higher, at the same time, the temperature in the motor is higher. So it is very important to calculate the thermal field of the motor and get the conclusion for the choice of the motor parameters. Reference [9], thermal network method and finite element method were respectively used to calculate the temperature distribution of automotive induction motors, and the calculation results were verified.

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Reference [10], the temperature of the fixed-frequency dual-rotor permanent magnet wind turbine was calculated by means of thermal network. The reference [11] proposed that the heat network and loss of the fluid network were combined to calculate the temperature rise of the synchronous generator with an empty cold water wheel. Reference [12] conducted joint simulation analysis of electromagnetic and thermal models of permanent magnet motors and induction motors. Reference [13] studies the thermal field of a high speed generator using the thermal network method, and obtains the average temperature rise of each component. Reference [14], the fluid-solid coupling method was used to analyze the temperature rise of permanent magnet motor, and computational fluid dynamics method was used to analyze the flow and heat transfer of air gap and end fluid. Reference [15] presents the criteria of the pole-slot numbers combination of the interior and surface permanent magnet synchronous machines with fractional-slot concentrated windings.

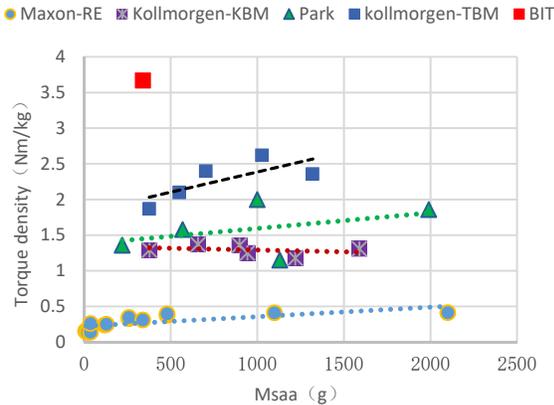


Fig. 2. Torque density contrast

A high torque density joint motor for humanoid robot is studied by the Group in this paper. In section II, the influence of key parameters on electromagnetism performance is analyzed, including the influence of polar arc coefficient and air gap length on torque and thermal load. In section III, the thermal network analysis model of the motor is established. The temperature rise of the motor is simulated by thermal network method and finite element method respectively. In section IV, a prototype is fabricated, and the experimental platform of the prototype system is built. The torque performance and the temperature rise of the motor are tested.

## II. ANALYSIS OF KEY PARAMETERS

The performance of the motor is affected by air gap length and the polar-arc coefficient of permanent magnet, here, the finite element analysis method has been used to establish the analysis model of the motor which is shown as Fig. 3. Simulation of motor performance under different parameters is carried out, and the variation trend of the torque and thermal load of the motor with the change of parameters is summarized. From Fig. 4, in the case of air gap is 0.2

and 0.3, the polar arc coefficient increases while the torque decreases, it is because the magnetic field is saturated. And while the air gap is 0.4, 0.5 and 0.6, the torque is increased with the increase of polar arc coefficient, it is because of the large magnetic resistance of air gap, the magnetic density is decreased, therefore, has not caused magnetic density is not saturation in the case of the polar arc coefficient is greater than 0.75. From Fig. 5 the thermal load is decreased as the polar arc coefficient is increased, it's because the magnetic flux goes up and the power stays the same, the increase of the magnetic load reduces the electric load, so the heat load goes down. To sum up, for this type of motor, the polar arc coefficient should be between 0.73 and 0.76.

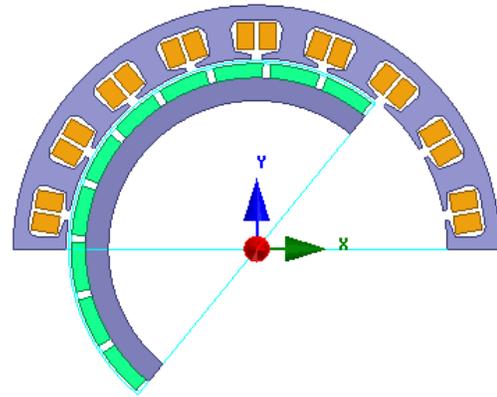


Fig. 3. Surface mounted magnetic pole structure

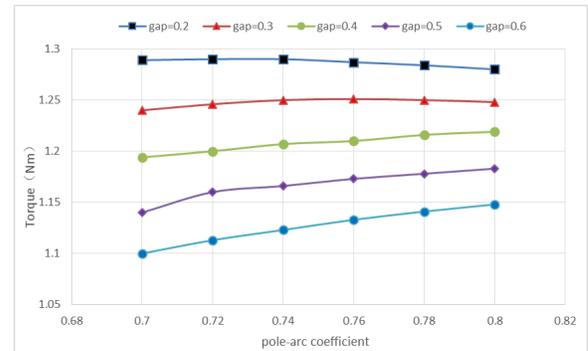


Fig. 4. The varies of torque with polar arc coefficient under different air-gap

## III. LUMPED PARAMETER THERMAL NETWORK MODELING AND ANALYSIS OF TEMPERATURE RISE

### A. Lumped parameter thermal network modeling

Radial modeling of the motor is shown as the Fig. 6, the heat source of the stator is produced by the stator teeth and yoke, the heat of the conductors in the slot consists of three heat sources. In order to calculate the uneven phenomenon of temperature rise in the slot, the heat of the winding is equivalent to three RC network series, calculate the temperature difference in the slot equivalent to a simplified

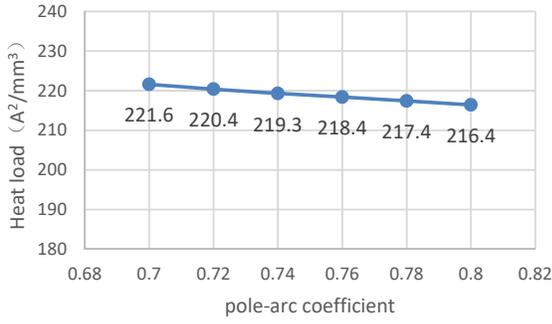


Fig. 5. The varies of thermal load with polar arc coefficient

layered structure. The heat in the stator and the slot is radially transmitted to the outside of the housing by the stator, and then, dissipated by convection of air. The heat source of rotor represents the eddy loss of permanent magnet, the rotating air on the permanent magnet surface is calculated by equivalent thermal resistance or heat transfer coefficient. On the one hand, permanent magnet heating is transmitted from the rotor yoke to the outside through the motor shaft, and on the other hand, when the surface temperature is higher than the stator tooth top, air gap may transfer heat to the stator, and if the surface temperature is lower than the stator tooth, the heat is transferred from the stator to the permanent magnet.

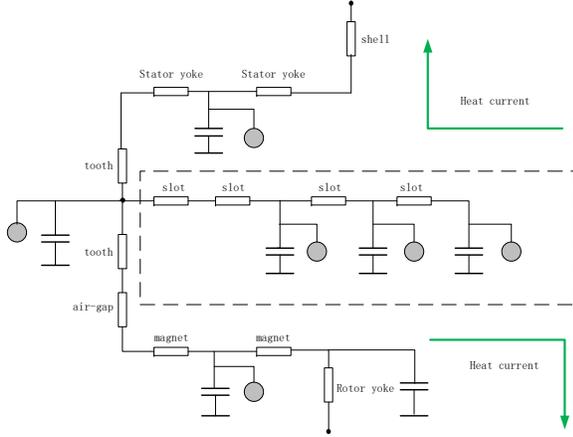


Fig. 6. Radial heat transfer diagram of motor

Thermal path parameters can be calculated from Eq. (1)-(6), here,  $h$  is convective heat transfer coefficient,  $S$  is surface area,  $A$  is Cross-sectional area,  $\lambda_v$  is longitudinal thermal conductivity of materials,  $d$  is the air gap length,  $l_0$  is the thickness of the core,  $D_1$  and  $D_2$  is diameter of bearing inner and outer ring,  $\omega$  is bearing width.

$$R_{Cu-air} = (hS)^{-1}/2 \quad (1)$$

$$R_{air-Cap} = (hA)^{-1}/2 \quad (2)$$

$$R_{Meg-Fe} = d/(\lambda_v S) \quad (3)$$

$$R_{Fe-air} = (hA)^{-1}/2 + l_0(\lambda_v A)^{-1} \quad (4)$$

$$R_{shf} = l_{end}(\lambda_v A)^{-1}/2 + l_0(\lambda_v A)^{-1} \quad (5)$$

$$R_{Bear} = d[(\lambda_v \pi D_1 \omega)^{-1} + (\lambda_v \pi D_2 \omega)^{-1}] \quad (6)$$

### B. Temperature calculation of the motor

The heat network model is established as shown in the Fig. 7, the magneto-thermal coupling analysis of the motor was carried out based on the heat path model by the iterative calculation. The electromagnetic calculation module is used to calculate the loss of each part of the motor at normal temperature, then, the loss value is imported into the temperature calculation module to calculate the temperature distribution of each area of the motor, more over we come back to the electromagnetic module to calculate the loss value of each part of the motor under the temperature distribution. The above process is iterated to obtain the convergence of motor temperature distribution and the loss of each part.

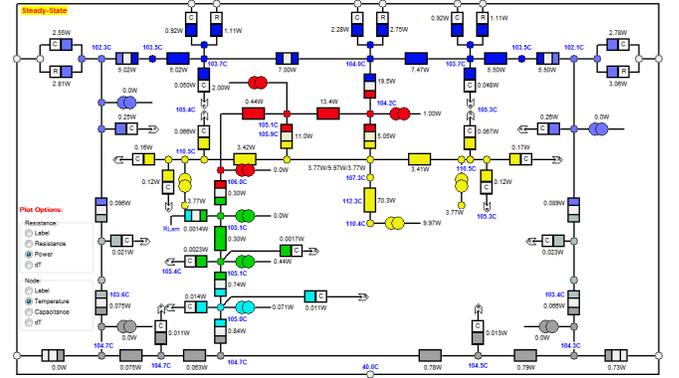


Fig. 7. Lumped parameter thermal network model of the motor

Fig. 8 shows the temperature distribution of each part of the motor after reaching thermal balance calculated by the heat path method, from the Fig. 8, the surface temperature of permanent magnet is 105°C, which will not cause permanent magnet demagnetization. Winding is the main factor of heating during motor operation, it can be seen from the figure that the maximum temperature of the winding is 119.5°C and the average temperature is 117.9°C. Fig. 9 shows the temperature rise of the motor winding after reaching thermal balance by using finite element method, the maximum temperature of the winding is 117°C, and the results of the two methods are consistent.

## IV. THE EXPERIMENT

A torque motor is designed, and the prototype is shown in Fig. 10. In order to test the load performance of the prototype and the temperature rise during the operation of the prototype, a motor test platform is built in this paper as shown in Fig. 11. The test platform is mainly consisted of the following parts: the motor to be tested, the driver,

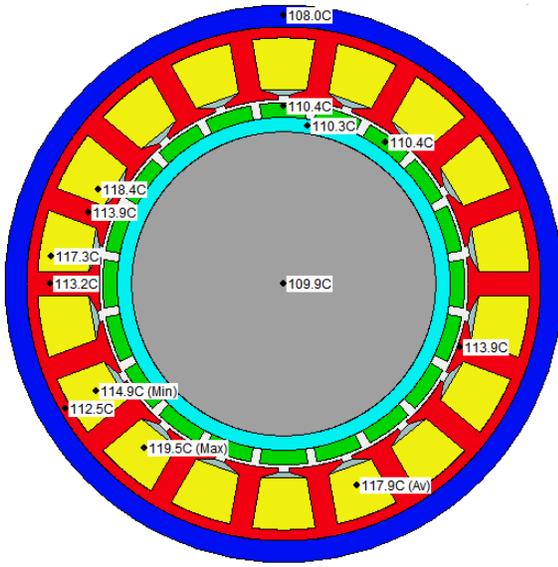


Fig. 8. Temperature distribution of the motor



Fig. 10. Prototype machine for test

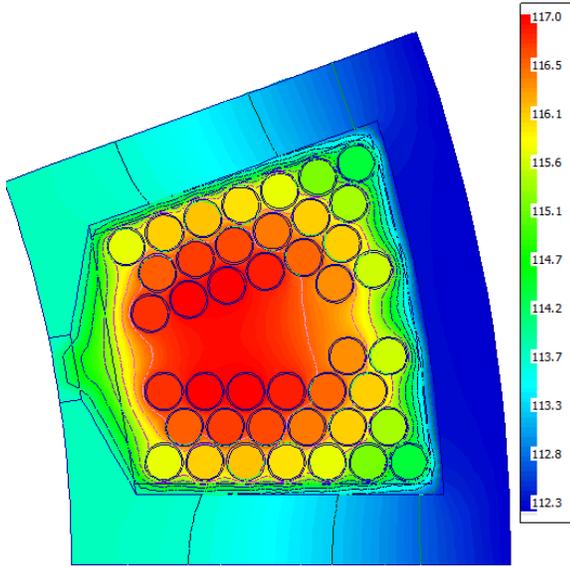


Fig. 9. Temperature distribution of winding

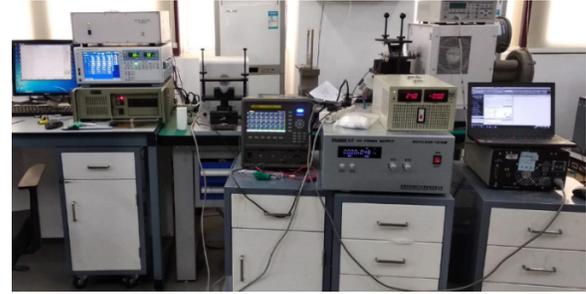


Fig. 11. The experiment platform

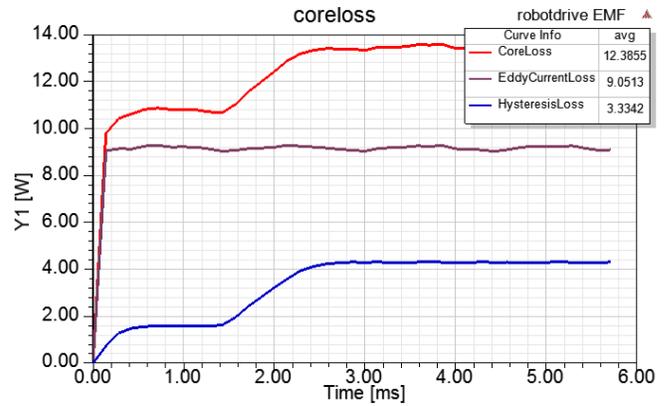


Fig. 12. Core loss curve

the ac intelligent load, the load controller, the speed-torque sensor, the power analyzer and the temperature measuring instrument.

Fig. 12 is the core loss curve of the motor. From the loss curve, after the motor has been steady running, the core loss is 12.3855w, the vortex loss 9.0513w, the hysteresis loss 3.3342w, total loss is 24.77w at 20°C. The rated power is 275w, therefore the max efficiency of the motor is 90.9%.

Fig. 13 is the induction voltage of the windings. Calculate the current according to the losses which have been shown in Fig. 7:

$$I = \sqrt{\frac{P_{cu}}{3R_{\varphi}}} = \sqrt{\frac{24.77}{3 \times \frac{0.655}{2}}} \approx 4.95A$$

$$p\psi_f = \frac{T}{I} = \frac{T}{\sqrt{3}I_q} = \frac{1.25}{1.732 \times 4.95} = 0.146$$

Therefore, the no-load line induction voltage is

$$E = \omega\psi_f = \frac{2\pi pn}{60} \times \frac{p\psi_f}{p} \approx 32V$$

The results computed by the analytical method are consistent with the results computed by the experimental data as shown in Fig. 13, which prove the feasibility of the design method.

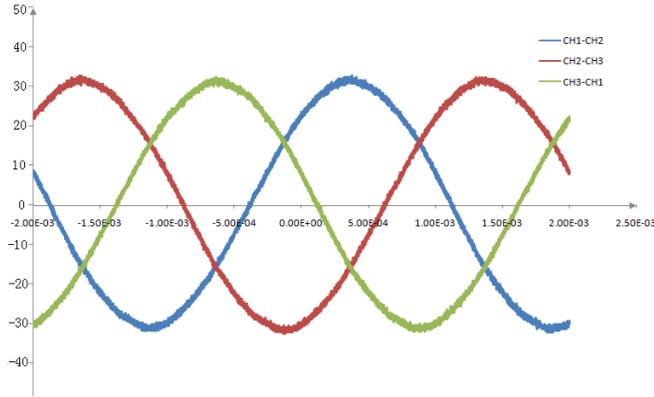


Fig. 13. Induction voltage of the windings

The motor worked at the rated voltage by the driver, the peak torque of the motor is 4.2Nm, based on the experimental platform as shown in the Fig. 11, from 0Nm to 4.5Nm, increase the load every 5 seconds, and each additional step is 0.2Nm. Fig. 14 is the torque-current curve of the motor, experimental results show that, the actual torque performance of the motor can reach the target of our design.

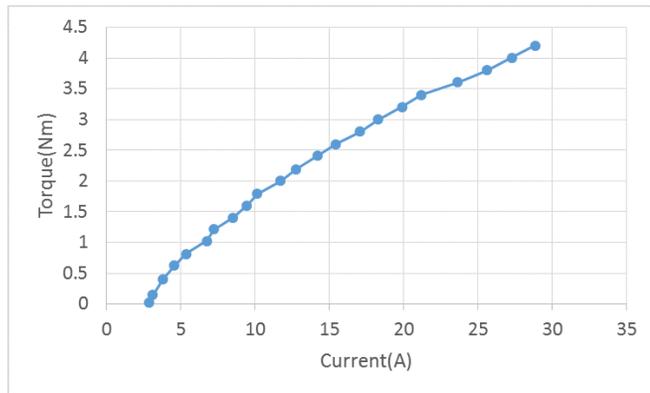


Fig. 14. Torque-current curve

The heat-sensitive resistance PT100 is embedded at the end of the winding, and the motor is cooled by natural cooling, the actual temperature value of motor winding is displayed by temperature measuring instrument during the operation of the motor. Table 1 shows the temperature which is and obtained by thermal network method and finite element method and experimental values, and the Fig. 15 is the temperature rise curve of the winding. The results of the thermal network method and finite element method are compared with the experimental data, the error of winding temperature is respectively 3.5% and 1.7%, the validity of theoretical calculation is proved, and at the same time, the actual temperature rise of the motor is 115.5°C, the temperature rise of the motor is well, so it can guarantee

safe operation under the allowed insulation condition.

TABLE I  
CALCULATED RESULTS AND MEASURED DATA

Comparison items	Different ways		
	thermal network	finite element	experimental value
Winding temperature rise °C	119.5	117	115.5

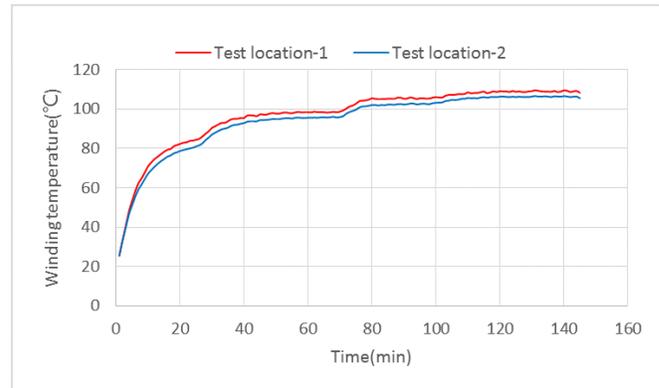


Fig. 15. Temperature rise curve

## V. CONCLUSIONS

A high torque density joint motor for humanoid robot is designed by the group, the influence of key parameters on electromagnetism performance is analyzed, and it has important significance to electromagnetic design for BLDC with similar rotor structure. The thermal network model is established, the magneto-thermal coupling analysis of the motor was carried out, the maximum temperature of the winding is 119.5°C and the average temperature is 117.9°C. By using finite element method, the maximum temperature of the winding is 117°C, and the results of the two methods are consistent. Experimental results show that, the actual torque performance of the motor can reach the target of our design, the torque density of the designed motor is 3.65Nm/kg. The actual temperature rise of the motor is 115.5°C, it can guarantee safety operation under the allowed insulation condition. In the future, we will apply this motor to our own humanoid robot, so as to improve the dynamic performance of the robot.

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